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Solutions

- (1) Use synthetic division to perform the division. $(2x^3 - 9x^2 + 10x - 3) \div (x - 3)$

Solutions.

The coefficients of $2x^3 - 9x^2 + 10x - 3$ are 2 for x^3 , -9 for x^2 , 10 for x , -3 for the free term. We divide by $x - 3$, so in the synthetic division, we use 3. We have the following table:

$$\begin{array}{r|rrrr}
 & x^3 & x^2 & x & \text{free} \\
 3 & 2 & -9 & 10 & -3 \\
 & \nearrow & 6 & \nearrow & -9 & \nearrow & 3 \\
 \hline
 & 2 & -3 & 1 & \boxed{0}
 \end{array}$$

Therefore, the quotient has the coefficients 2, -3 , and 1, and it starts with the power x^2 (one degree less): $2x^2 - 3x + 1$. The last number, 0, is the remainder. ■

- (2) Is $x + 1$ a factor of $P(x) = x^3 + 2x^2 - 2x - 3$? Use **ONLY** the **Factor Theorem** (beware that this is not the factorization we learned in previous chapters).

Solutions.

The **Factor Theorem** states that $x - r$ is a factor of the polynomial $P(x)$ **if and only if** $P(r) = 0$.

$r = -1$ in our case, because $x + 1 = x - (-1)$. Then,

$$P(-1) = (-1)^3 + 2 \cdot (-1)^2 - 2 \cdot (-1) - 3 = -1 + 2 + 2 - 3 = 0 \quad .$$

Then, according to the Factor Theorem, $x + 1$ is a factor of $P(x) = x^3 + 2x^2 - 2x - 3$, because $P(-1) = 0$. ■

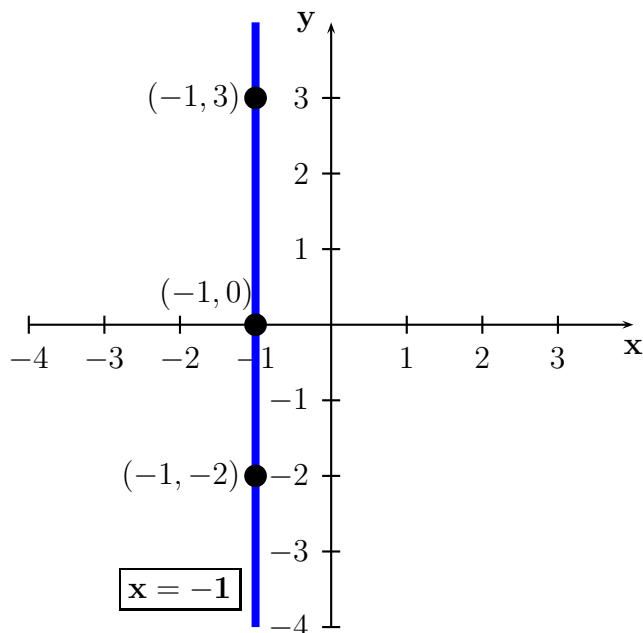
- (3) Draw the line $x = -1$.

Solutions.

The line $x = -1$ is a vertical line (all points with the x -coordinate equal to -1 , i.e. the y -coordinate can be everything):

x	y
-1	-2
-1	0
-1	3

So, we graph the vertical line that passes through the points $(-1, -2)$, $(-1, 0)$, and $(-1, 3)$. Here is the graph:



- (4) What is the slope of the line passing through the points $(0, -8)$ and $(-5, 0)$.

Solutions.

The definition of the slope of the line passing through the points (x_1, y_1) and (x_2, y_2) is:

$$m = \frac{y_2 - y_1}{x_2 - x_1} .$$

Let choose $(x_1, y_1) = (0, -8)$ and $(x_2, y_2) = (-5, 0)$. Then, the slope of our line is:

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{0 - (-8)}{-5 - 0} = \frac{0 + 8}{-5} = -\frac{8}{5} . \blacksquare$$