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Solutions

- (1) Use synthetic division to perform the division. $(3x^3 - 10x^2 + 5x - 6) \div (x - 3)$

Solutions.

The coefficients of $3x^3 - 10x^2 + 5x - 6$ are 3 for x^3 , -10 for x^2 , 5 for x , -6 for the free term. We divide by $x - 3$, so in the synthetic division, we use 3 . We have the following table:

$$\begin{array}{r|rrrr}
 & x^3 & x^2 & x & \text{free} \\
 3 & 3 & -10 & 5 & -6 \\
 & \nearrow & 9 & \nearrow & -3 & \nearrow & 6 \\
 \hline
 & 3 & -1 & 2 & \boxed{0}
 \end{array}$$

Therefore, the quotient has the coefficients 3 , -1 , and 2 , and it starts with the power x^2 (one degree less): $3x^2 - x + 2$. The last number, 0 , is the remainder. ■

- (2) Is $x + 2$ a factor of $P(x) = x^3 + 3x^2 - x - 6$? Use **ONLY** the **Factor Theorem** (beware that this is not the factorization we learned in previous chapters).

Solutions.

The **Factor Theorem** states that $x - r$ is a factor of the polynomial $P(x)$ **if and only if** $P(r) = 0$.

$r = -2$ in our case, because $x + 2 = x - (-2)$. Then,

$$P(-2) = (-2)^3 + 3 \cdot (-2)^2 - (-2) - 6 = -8 + 12 + 2 - 6 = 0 \quad .$$

Then, according to the Factor Theorem, $x + 2$ is a factor of $P(x) = x^3 + 3x^2 - x - 6$, because $P(-2) = 0$. ■

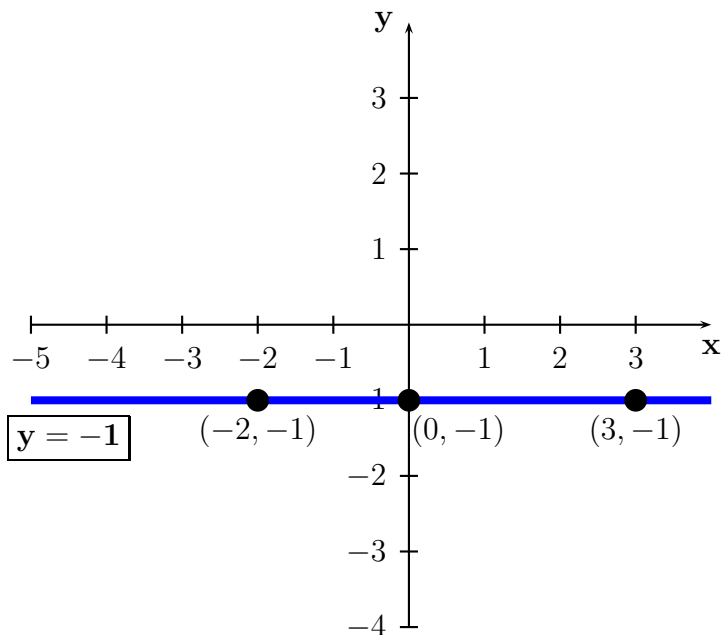
- (3) Draw the line $y = -1$.

Solutions.

The line $y = -1$ is a horizontal line (all points with the y -coordinate equal to -1 , i.e. the x -coordinate can be everything):

x	y
-2	-1
0	-1
3	-1

So, we graph the vertical line that passes through the points $(-2, -1)$, $(0, -1)$, and $(3, -1)$. Here is the graph:



(4) What is the slope of the line passing through the points $(2, -8)$ and $(-1, 0)$.

Solutions.

The definition of the slope of the line passing through the points (x_1, y_1) and (x_2, y_2) is:

$$m = \frac{y_2 - y_1}{x_2 - x_1} .$$

Let choose $(x_1, y_1) = (2, -8)$ and $(x_2, y_2) = (-1, 0)$. Then, the slope of our line is:

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{0 - (-8)}{-1 - 2} = \frac{0 + 8}{-3} = -\frac{8}{3} . \blacksquare$$